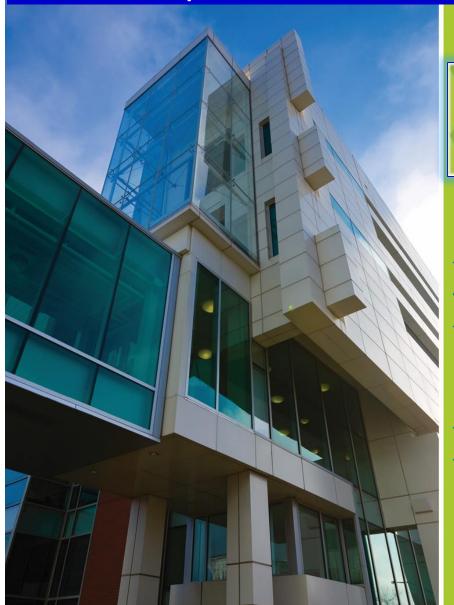


Materials Informatics: Mining and Learning from Data for Accelerated Design and Discovery

Krishna Rajan

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Dept. Materials Design and Innovation





http://engineering.buffalo.edu/materials-design-innovation.html

http://www.cas.buffalo.edu/depart
ments-programs/

krajan3@buffalo.edu

A new paradigm - computational and experimental materials science + Big Data







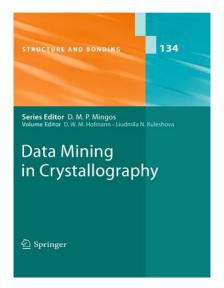


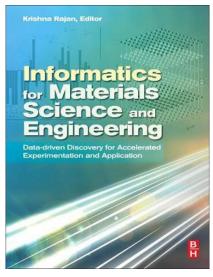
"Optics" of Data

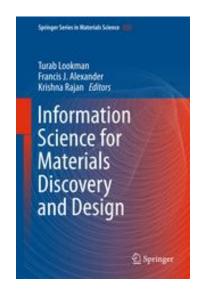




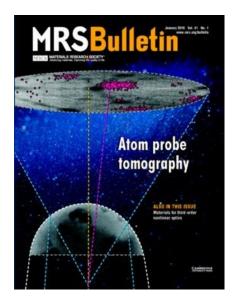
Bibliography

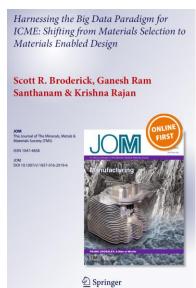


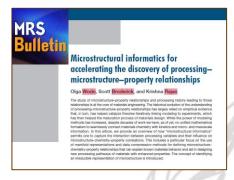


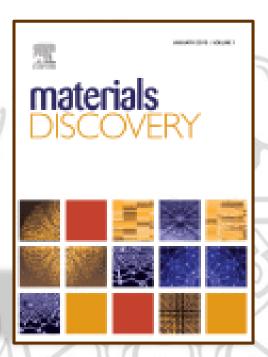




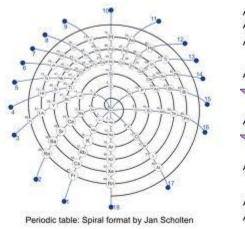


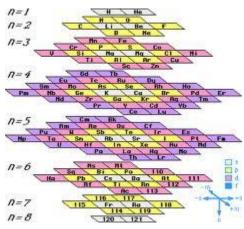


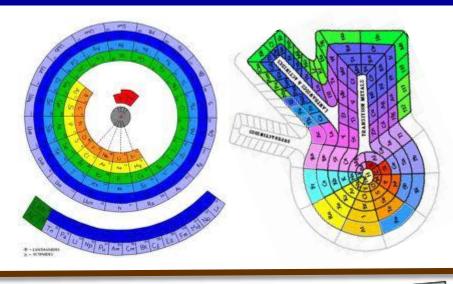




Cartography for Materials : *mapping elemental characteristics*









опыть системы элементовъ.

основанной на наъ атомномъ въсъ и химическомъ сходствъ.

Ti-So Zr = 90 ?-180.

V-51 Nb- 94 Ta-182.

Cr-52 Mo- 96 W-186.

Mn-55 Rh-104,4 Pt-197,1
Fe=56 Rn-104,4 Ir-198.

NI-Co=59 PI-106,5 O-=199.

Cu-63,4 Ag-108 Hg-200.

Be= 9,4 Mg-24 Zn-65,2 Cd-112
B=11 Al-27,4 ?-68 Ur-116 Au-197?

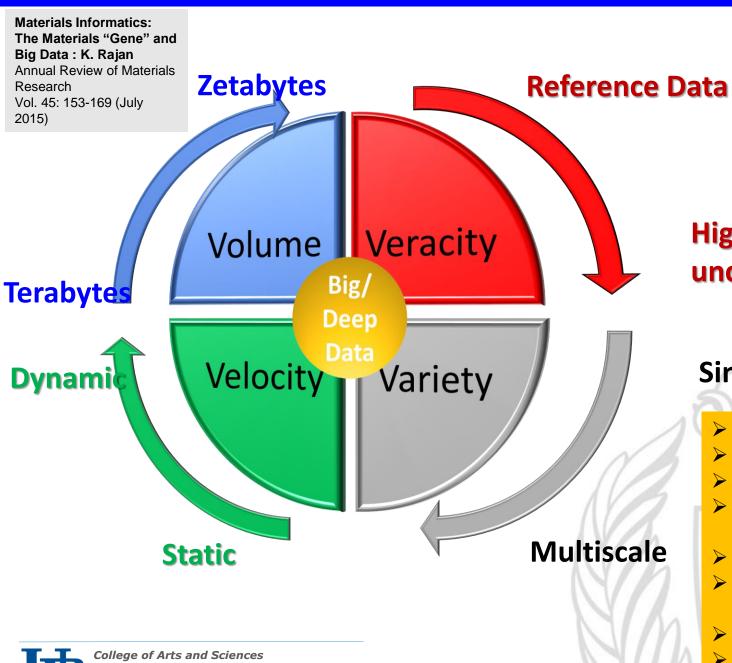
C=12 Si-28 ?-70 Sn-118
N=14 P-31 As-75 Sb=122 BI-210?
0=16 S-32 Se-79,4 Te-128?
F=19 CI-35,6 Br-80 I-127
=7 Na-23 K=39 Rb-85,4 Cs=133 TI-204.
Ca-40 Sr-87,6 Ba-137 Pb=207.
?-45 Ce-92
?Er-56 La-94
?Y1-60 Di-95
?In-75,6 Th-118?

Д. Мендальовъ

																	2
																	Не
1												5	6	7	8	9	10
H 3	4	le.										В	С	N	0	F	Ne
نا	Be											13	14	15	16	17	18
11	12											Al	Si	р	s	Cl	Ar
Na	Mg	L			- 24	25	26	27	28	29	30	31	32	33	34	35	36
19 K	Ca	Sc 21	Ti	23 V	Cr	25 Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
37	38	_	_	_	42		_		_	_	48	49	50	51	52	53	54
Rb	Sr	Υ	Zr	Nb	Мо	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
55		57	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
Cs	Ba	•	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	TI	Pb	Bi	Po	At	Rn
87 Fr.	Ra	89			106				110		_		114	115		117	118
1		_	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Uub	Uut	Uuq	Uup	Uuh	Uus	Uuo
		57	58	59	60	61	62	63	-		_						300
		la	Ce	Pr	Nd		Sm	Eu					68	69	70	71	
		89	90	91	_		_		Gd	Tb	Dy	Но	Er	Tm	Yb	In.	

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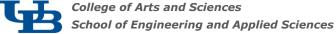
MDI for "Knowledge Bases" vs Data Bases



High levels of uncertainty

Single scale

- Crystallography
- Metrology/ Sensing
- Biopolymer design
- Chemical design of nanostructures
- Catalysis
- Alloy discovery and design
- Composites
- Decision systems in materials engineering



Outline

- > Formatting the inverse design problem as a data mining problem
- ➤ Defining the concept of "data" in materials sciencemathematical framework for materials design via statistical learning: materials informatics
- > Applications in crystal chemistry design



Inverse Design: an informatics/ data mining perspective

- **➤** Discovering classifiers:
 - ➤ Can we trace and identify key characteristics of a material that distinguishes key differences in a materials behavior
- ➤ Ranking descriptors:
 - ➤ Can we trace back and discover key parameters or correlations of parameters without explicitly knowing the forward design problem?

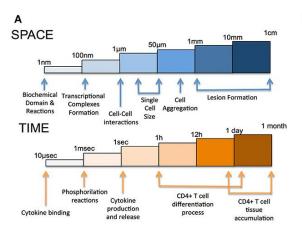
Informatics for materials discovery

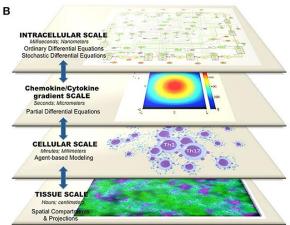
- ➤ Data driven discovery with limited or uncertain information
- ➤ Data from different sources---
 - ➤ How can we deal with training and test data from different distributions?
 - ➤ What can be learned when a classifier (or predictor) is used outside of the domain of training?
 - ➤ Can we build classifiers?

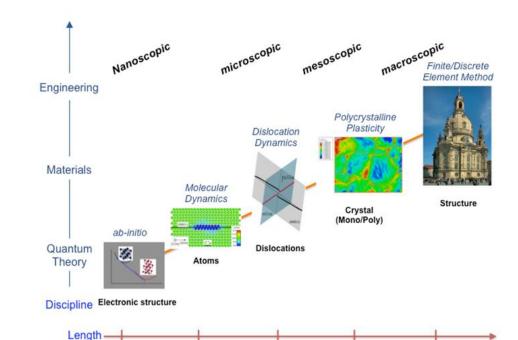
Establishing predictive materials science through data science

"Multiscale Perspective

http://www.frontiersin.org/files/Articles/101961/fcell-02-00031-HTML/image m/fcell-02-00031-g003.jpg





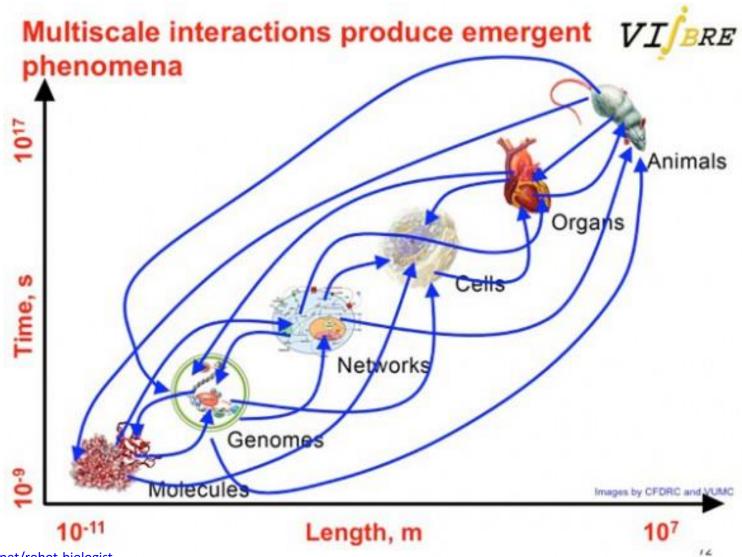


http://tu-freiberg.de/international-master-in-computational-materials-science/multiscale-modeling

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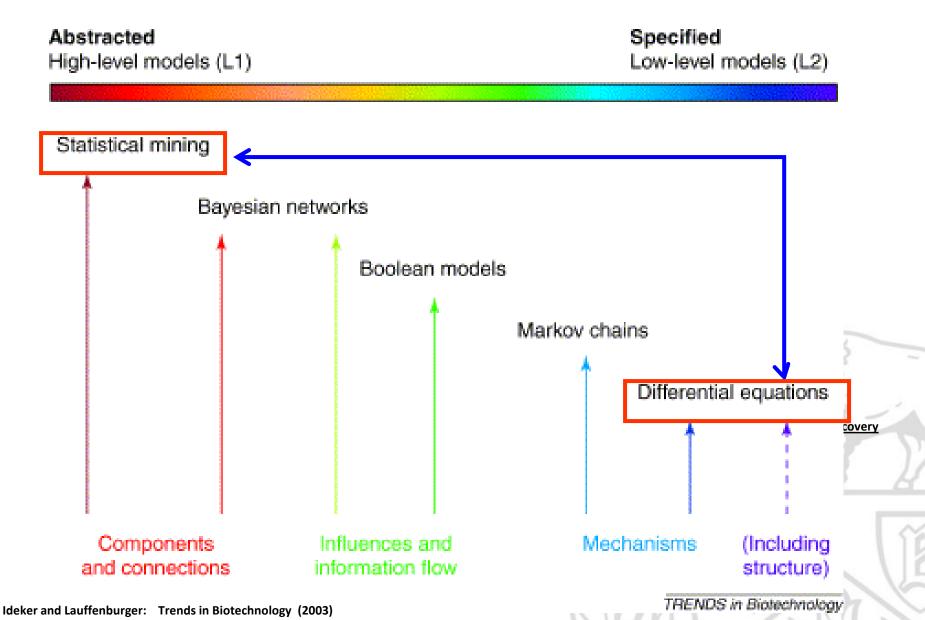
"Multiscale Perspective



http://www.kurzweilai.net/robot-biologist-solves-complex-problem-from-scratch



"Omics in Materials Science



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Functionality =
$$\mathcal{F}(x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8, \dots)$$

Issues:

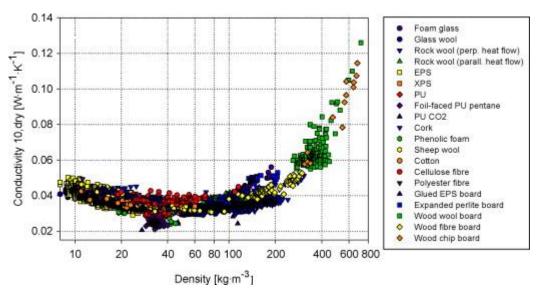
- how many variables?
- which variables are important?
- classify behavior among variables
- making quantitative predictions ...relate functionality to variables ...
 - traditionally we describe them by empirical equations:
 - Quantitative Structure Activity Relationships (QSARs) are derived from data mining techniques not assuming a priori which physics is the most important

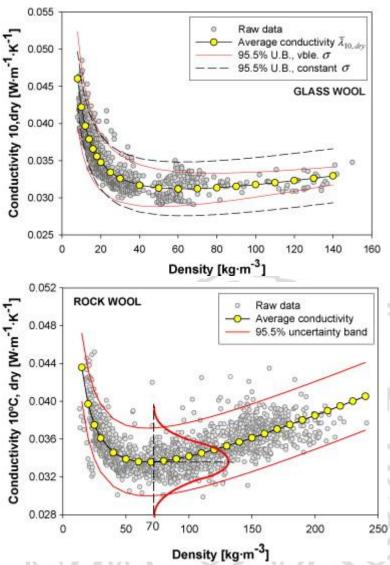
Need to build database with these variables

- Need to establish a genomics-proteomics-metabolomics etc.: Systems
 Biology approach
- What are the data management and sharing issues for a systems approach?

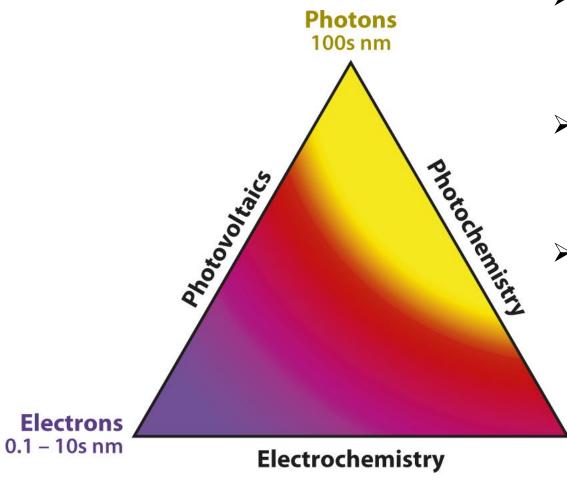
Uncertainty in Materials Behavior

<u>Uncertainty in the thermal conductivity of insulation materials</u> Original Research Article Energy and Buildings, Volume 42, Issue 11, November 2010, Pages 2159-2168 Fernando Domínguez-Muñoz, Brian Anderson, José M. Cejudo-López, Antonio Carrillo-Andrés





Discovery Challenge



- Challenges in materials
 discovery sparse information
 search space prohibitive
- Informatics aided combinatorial experiments and high throughput computation
- Statistical learning- explore parameter space outside computational / experimental bounds

Chemical bonds 0.1 nm

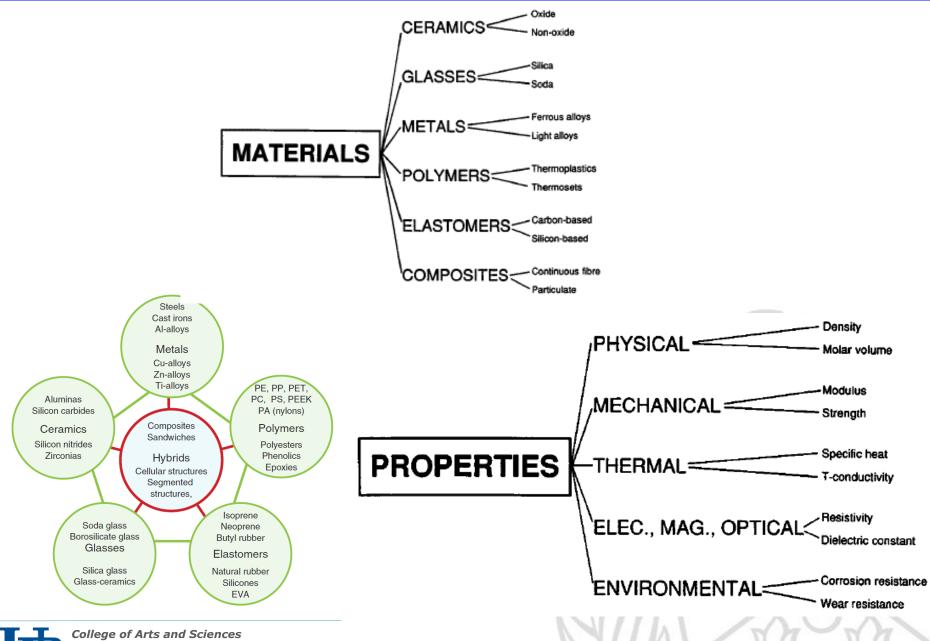
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Crabtree G, Sarrao J. 2011.

Annu. Rev. Condens. Matter Phys. 2:287-301

CLASSIFICATION:

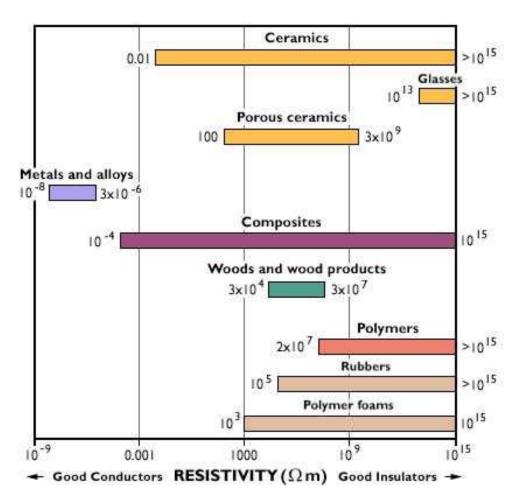
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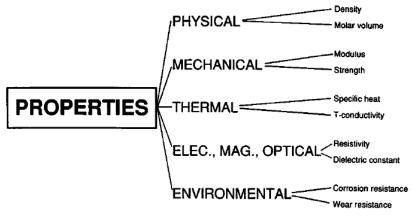


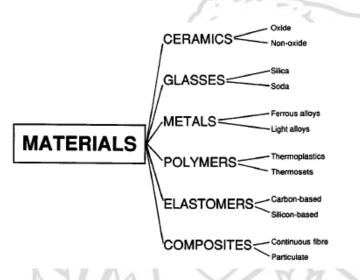
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ASSOCIATION: Krishna Rajan

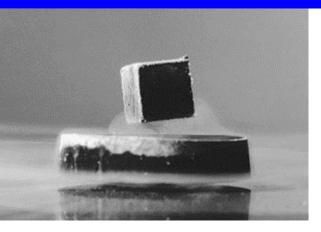






OUTLIER DETECTION:

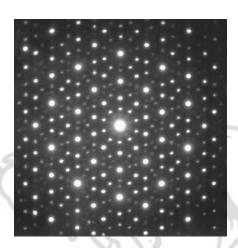
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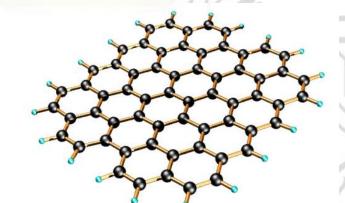




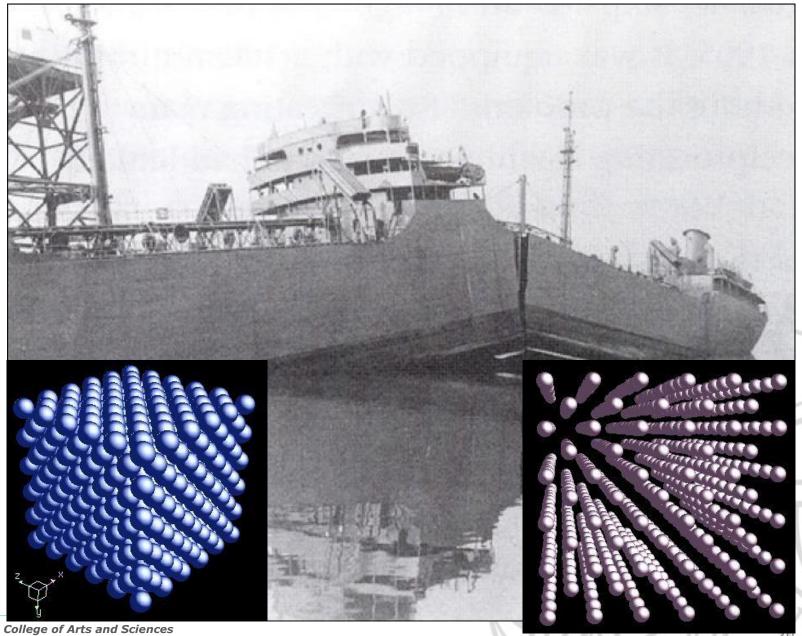








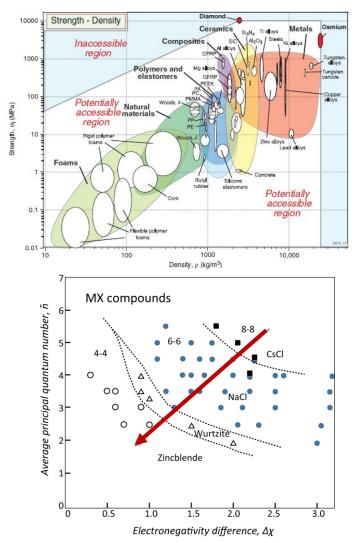
ASSOCIATION MINING



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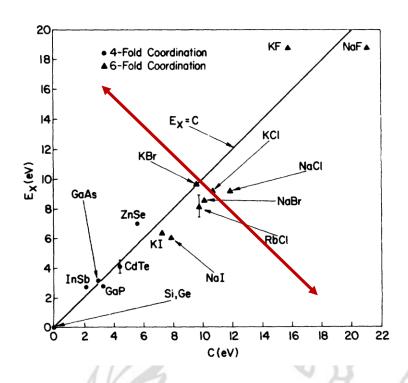
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CLUSTERING: Krishna Rajan



Nested clusters

Decision Boundary

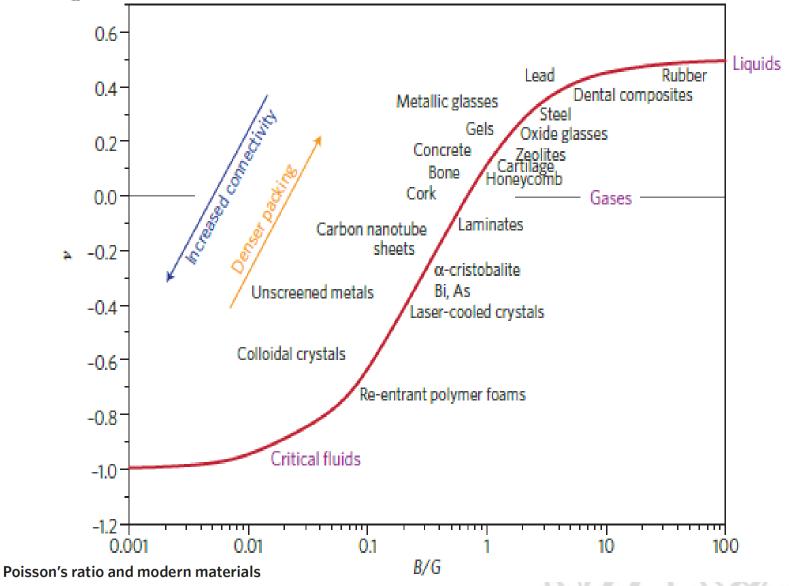


PHYSICAL REVIEW B VOLUME 8, 15 DEC. 1973
Atomic Pseudopotentials and the Ionicity Parameter of Phillips and Van Vechten
D. J. Chadi~ and Marvin L. Cohen* and D. Grobman

https://commons.wikimedia.org/wiki/File:Mooser-pearson.png



Data for Design



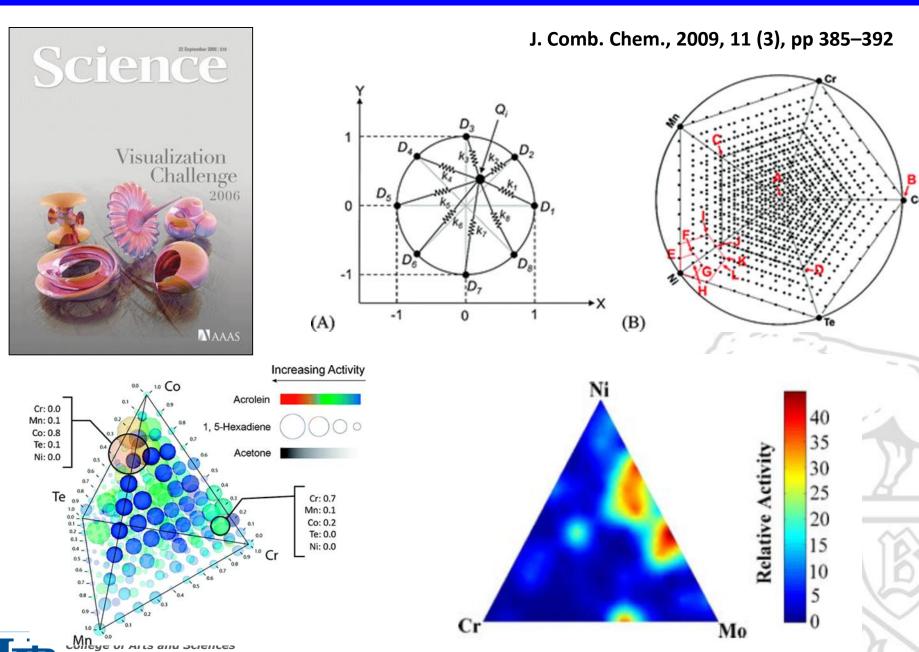
G. N. Greaves^{1,2*}, A. L. Greer¹, R. S. Lakes³ and T. Rouxel⁴

NATURE MATERIALS | VOL 10 | NOVEMBER 2011 | www.nature.com/naturematerials



Data Velocity: discovering catalyst chemistries

School of Engineering and Applied Sciences



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Discovering Classifiers

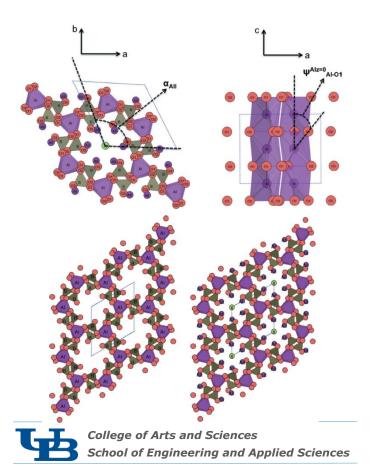
research papers

Acta Crystallographica Section B **Structural Science**

ISSN 0108-7681

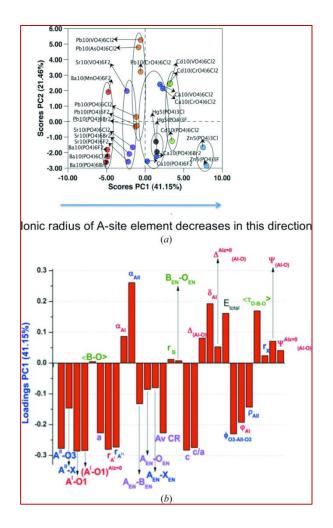
Structure maps for $A_4^{II}A_6^{II}(BO_4)_6X_2$ apatite compounds *via* data mining

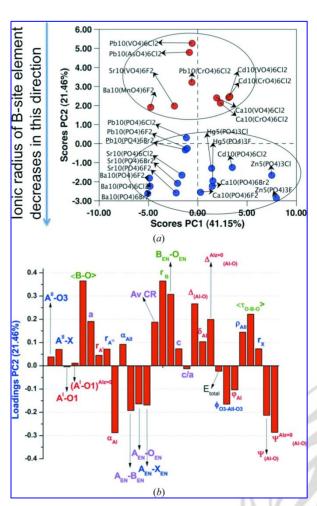
Prasanna V. Balachandran and Krishna Rajan*

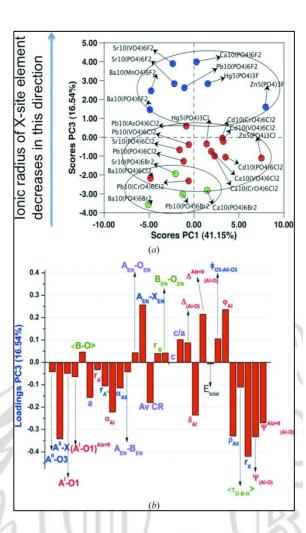


Descriptor	Brief description
a (Å)	
a (A) c (Å)	Lattice constant of the hexagonal unit cell Lattice constant of the hexagonal unit cell
c/a	Variable axial ratio (no unit)
$r_{\rm AI}$ (Å)	Shannon's ionic radii of A ^I -site ion (nine-coordination)
$r_{\rm B}$ (Å)	Shannon's ionic radii of <i>B</i> -site ion
r_{AII} (Å)	Shannon's ionic radii of A ^{II} -site ion (seven-coordination for F ⁻ and eight-coordination for Cl ⁻ and Br ⁻ ; Đorđević <i>et al.</i> , 2008)
$r_{\rm X}$ (Å)	Shannon's ionic radii of X-site ion
Av CR (Å)	Average crystal radius = $[(r_{AI}x4) + (r_{AII}x6) + (r_{B}x6) + (r_{O}x24) + r_{X}x2)]/42$
$A_{\rm EN}-{ m O}_{\rm EN}$	Electronegativity difference A atom and O atom
$B_{\mathrm{EN}}-\mathrm{O}_{\mathrm{EN}}$	Electronegativity difference B atom and O atom
$A_{\rm EN} - X_{\rm EN}$	Electronegativity difference A atom at A^{Π} site and X atom
$A_{\rm EN}-B_{\rm EN}$	Electronegativity difference A atom at A^{I} site and B atom
$A^{I} - O1 (\mathring{A})$ $A^{I} - O1^{AIz} = 0$ (\mathring{A})	Distance between A^{I} and O1 atom Distance between A^{I} and O1 atom with the constraint $z = 0$ at A^{I}
$\Delta_{\text{AI}-\text{O}} (\mathring{A})$ $\Delta_{\text{AI}-\text{O}}^{\text{AI}z=0} (\mathring{A})$	Difference in the lengths A^{I} —O1 and A^{I} —O2 Difference in the lengths A^{I} —O1 and A^{I} —O2 with
	the constraint $z = 0$ at A^{I}
$\psi_{ m AI-O}$ (°)	The angle that the $A^{\rm I}$ —O1 bond makes with respect to c
$\psi_{\mathrm{AI-O}}^{\mathrm{AI}z=0}$ (°)	The angle that the A^{I} —O1 bond makes with respect to c with the constraint $z = 0$ at A^{I}
$\delta_{ m AI}~(^\circ)$	Counter-rotation angle of A ^I O ₆ structural unit
$\varphi_{ m AI}$ (°)	Metaprism twist angle $(\pi/3 - 2\delta_{AI})$
$\alpha_{ m AI}$ (°)	Orientation of $A^{I}O_6$ unit with respect to a
$\langle B-O\rangle$ (Å)	Average <i>B</i> —O bond length
$\langle \tau_{\mathrm{O}-B-\mathrm{O}} \rangle$ (°)	Average $O-B-O$ bond-bending angle
$ \rho_{\text{AII}}(\mathring{\mathbf{A}}) $ $ A^{\text{II}} - X(\mathring{\mathbf{A}}) $	$A^{II} - A^{II}$ triangular side length
$A^{-}-X$ (A)	Distance between A^{II} and X atom
α_{AII} (°)	Orientation of $A^{II} - A^{II} - A^{II}$ triangles with respect to a
A^{II} – O3 (Å)	Distance between A^{II} and O3 atom O3- A^{II} -O3 angle
$\Phi_{\text{O3-AII-O3}}$ (°)	
E_{total} (eV)	Total energy calculated from ab initio calculations

Ranking Descriptors

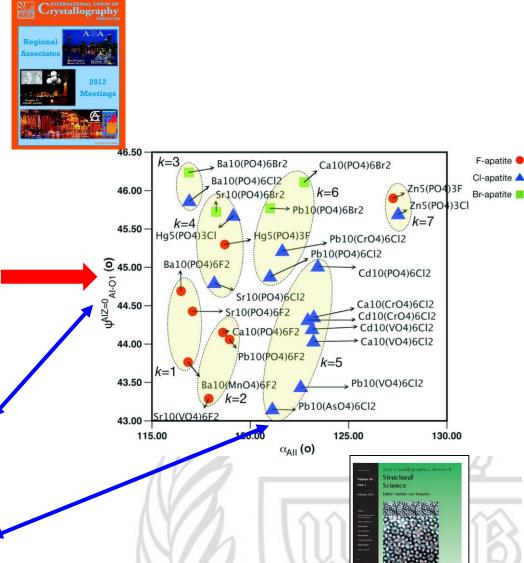






Structure Classification Maps from Data Mining

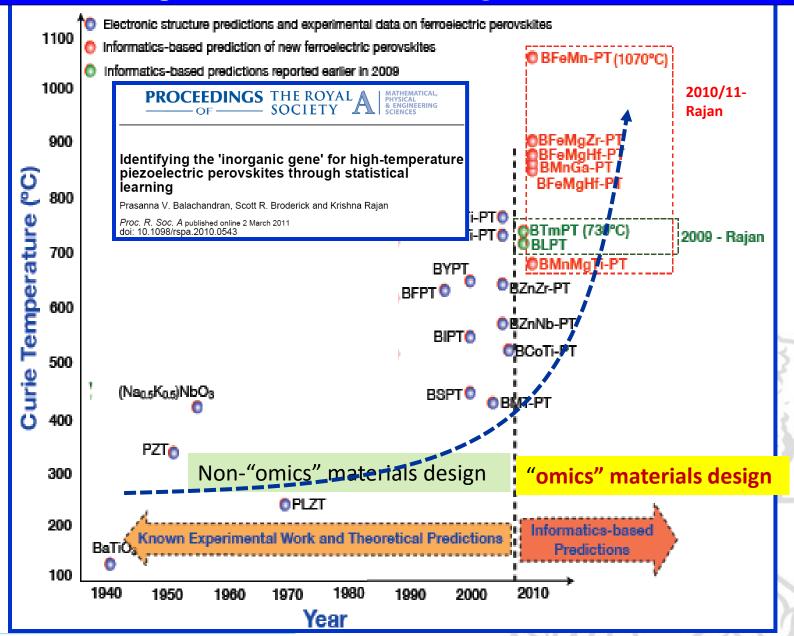
Descriptor	Brief description
a (Å)	Lattice constant of the hexagonal unit cell
c (Å)	Lattice constant of the hexagonal unit cell
c/a	Variable axial ratio (no unit)
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$r_{\rm B}$ (Å)	Shannon's ionic radii of <i>B</i> -site ion
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$A_{\rm EN} - {\rm O}_{\rm EN}$	Electronegativity difference A atom and O atom
$B_{\rm EN} - {\rm O}_{\rm EN}$	Electronegativity difference B atom and O atom
$A_{\rm EN} - X_{\rm EN}$	Electronegativity difference A atom at A^{II} site and X atom
$A_{\rm EN}-B_{\rm EN}$	Electronegativity difference A atom at A^{I} site and B atom
$A^{\rm I}$ $-$ O1 (Å)	Distance between A ^I and O1 atom
A^{I} $ O1$ (\mathring{A}) A^{I} $ O1^{\mathrm{AI}z=0}$	Distance between A^{I} and O1 atom with the
(Å)	constraint $z = 0$ at A^{I}
	Difference in the lengths A^{I} —O1 and A^{I} —O2
$\Delta_{ ext{AI}- ext{O}}\left(ext{Å} ight) \ \Delta_{ ext{AI}- ext{O}}^{ ext{AI}z=0}\left(ext{Å} ight)$	Difference in the lengths A^{I} —O1 and A^{I} —O2 with the constraint $z = 0$ at A^{I}
$\psi_{ m AI-O}$ (°)	The angle that the A^{I} -O1 bond makes with respect
. AIz = 0 (a)	to c
$\psi_{\text{AI}-\text{O}}^{\text{AI}z=0}$ (°)	The angle that the A^{I} —O1 bond makes with respect to c with the constraint $z = 0$ at A^{I}
δ_{AI} (°)	Counter-rotation angle of A O ₆ structural unit
φ _{AI} (°)	Metaprism twist angle $(\pi/3 - 2\delta_{AI})$
α _{AI} (°)	Orientation of $A^{I}O_{6}$ unit with respect to a
$\langle B-\mathrm{O}\rangle$ (Å)	Average <i>B</i> —O bond length
$\langle \tau_{\mathrm{O}-B-\mathrm{O}} \rangle$ (°)	Average $O-B-O$ bond-bending angle
ρ_{AII} (Å)	$A^{\mathrm{II}} - A^{\mathrm{II}}$ triangular side length
$A^{\text{ff}} - X(A)$	Distance between A ^{II} and X atom
α _{ΑΙΙ} (°)	Orientation of $A^{II} - A^{II} - A^{II}$ triangles with respect
4II 02 (Å)	to a
A^{II} – O3 (Å)	Distance between A^{II} and O3 atom
$\Phi_{\text{O3-AII}-\text{O3}}$ (°)	$O3-A^{II}-O3$ angle
E_{total} (eV)	Total energy calculated from ab initio calculations



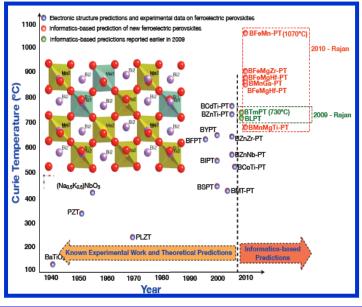


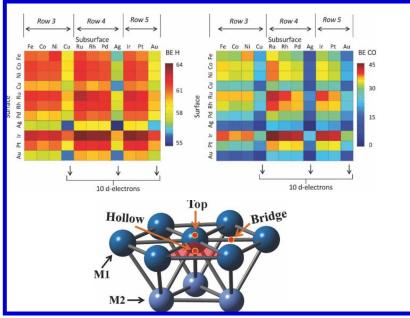
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Accelerated Design- value of "omics" design

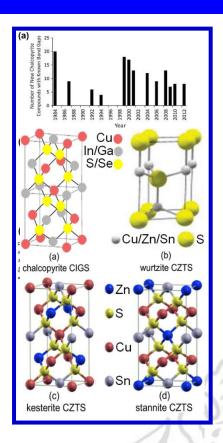


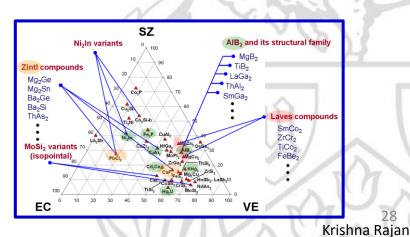
Informatics Driven Materials Discovery





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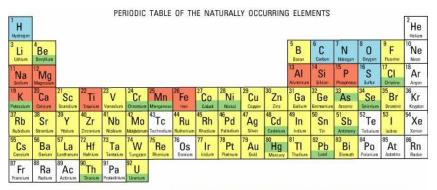


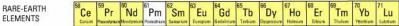


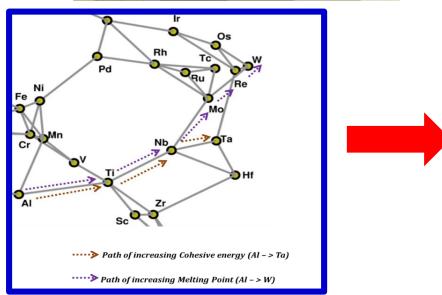
Discovering Chemical Pathways for Microstructure Sensitive Properties – Alloy Design



S.Srinivasan et.al. **5**,17960 doi:10.1038/srep17960(2015)







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School of Engineering and Applied Sciences

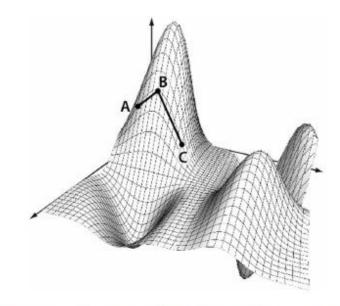


FIGURE 5 | Geodesic distance calculation. The distance between A and C is calculated as the manifold path distance from A to B to C, instead of the direct path from A to C. This eliminates the assumption that the points occupy a linear space when using a Euclidean distance.

1																	2
H																	He
3	4											5	6	7	8	9	10
Li	Be											В	C	N	0	F	Ne
11	12											13	14	15	16	17	18
Na	Mg											Al	Si	P	S	CI	Ar
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	ln	Sn	Sb	Te	1	Xe
55	56	57	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
Cs	Ba	La	Hf	Ta	W	Re	Os	lr	Pt	Au	Hg	TI	Pb	Bi	Po	At	Bn
87	88	89												-			
Fr	Ra	Ac															



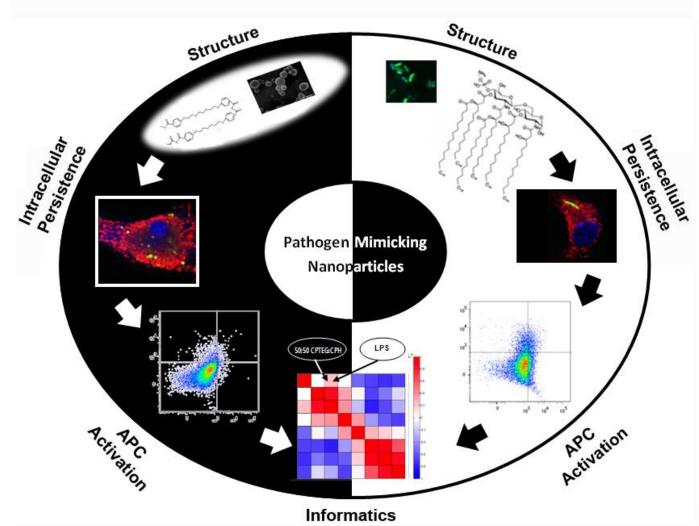
Data driven health delivery systems



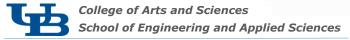


Rational Design of Pathogen-Mimicking Amphiphilic Materials as Nanoadjuvants

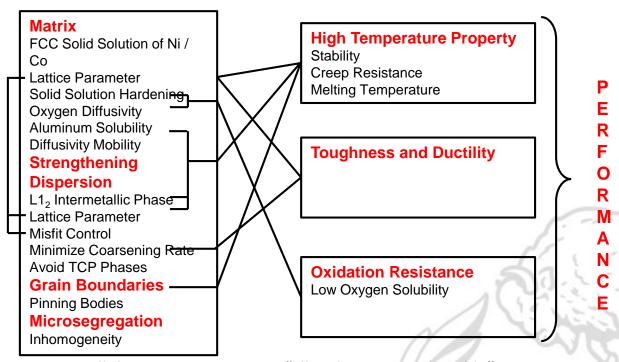
Ideal vaccine will mimic the way in which a naturally occurring infection induces a robust immune response yet avoid the undesirable effects of disease



Ulery et.al (2012)



Traditional Design Approach

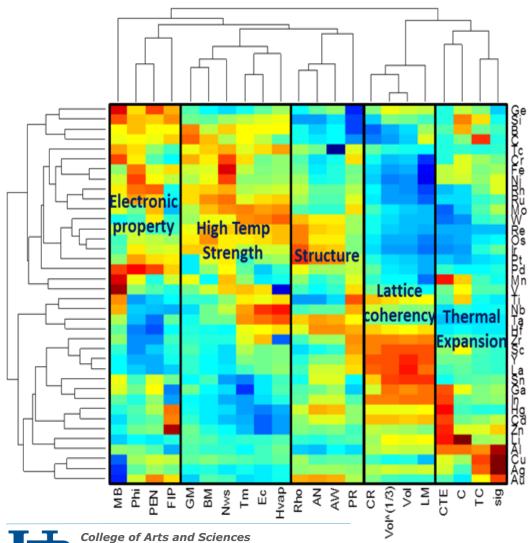


By integrating all the properties into our "alloy design periodic table", we capture the design minutia and make all of these connections without having to do all possible calculations and experiments we would otherwise sequentially do.

Chemical similarity / dissimilarity and materials design

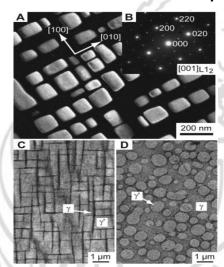


S.Srinivasan et.al. **5**,17960 doi:10.1038/srep17960(2015)



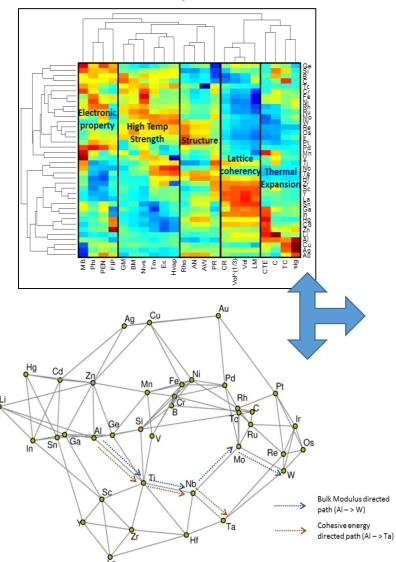
Design constraint – intermetallic chemistry that impacts microstructural level properties :

- L12
- Lattice misfit-
- High temperature strength – modulus / cohesive energy-"Dissimilarity metric"



Advances in Methodology

Graph traversal

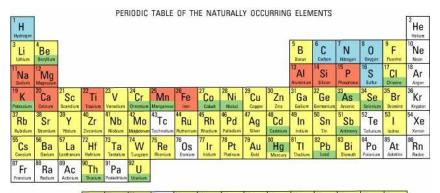


Start	Nearest Neighbor	Enthalpy of Formation	Cohesive Energy	Nearest Neighbor Map					
	Ga	-0.24	4.23	Zn /\					
Al	Si	-0.25	4.70	si					
AI	Ti	-0.31	4.82	Al Ga					
	Zn	-0.12	3.75	π					
	Al	-0.31	4.45						
	Ga	-0.24	4.23	Al-Ga Si					
	Hf	-0.40	5.31						
Ti	Nb	-0.27	5.45	Sc Nb					
	Sc	-0.34	4.61	30					
	Si	-0.25	4.70	Zr———Hf					
	V	-0.15	4.77	501:					
	Hf	-0.40	5.31	Mo					
NIP.	Мо	-0.05	5.05	TI					
Nb	Та	-0.27	5.59	Nb					
	Ti	-0.31	4.82	Ne la					
	Hf	-0.40	5.31	Mo Re					
_	Мо	-0.05	5.05						
Та	Nb	Nb -0.27		Nb					
	Re	0.02	5.28	H					

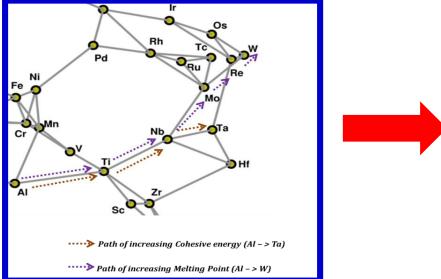
Discovering Chemical Pathways for Microstructure Sensitive Properties – Alloy Design



S.Srinivasan et.al. **5**,17960 doi:10.1038/srep17960(2015)







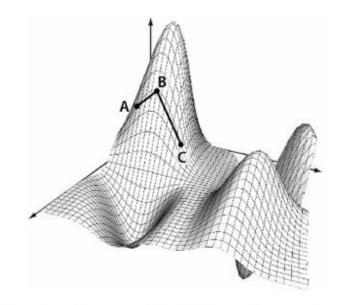


FIGURE 5 | Geodesic distance calculation. The distance between A and C is calculated as the manifold path distance from A to B to C, instead of the direct path from A to C. This eliminates the assumption that the points occupy a linear space when using a Euclidean distance.

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K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
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Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	ln	Sn	Sb	Te	1	Xe
55	56	57	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
Cs	Ba	La	Hf	Ta	W	Re	Os	lr	Pt	Au	Hg	TI	Pb	Bi	Po	At	Bn
87	88	89															
Fr	Ra	Ac															

Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Kr	ishn	a R	ajan
90													103
Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Но	Er	Tm	Yb	Lu
58	59	60	61	62	63	64	65	66	67	68	69	70	71

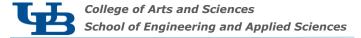


Image interpretation: "inverse problem"...mapping the gene

Challenge:

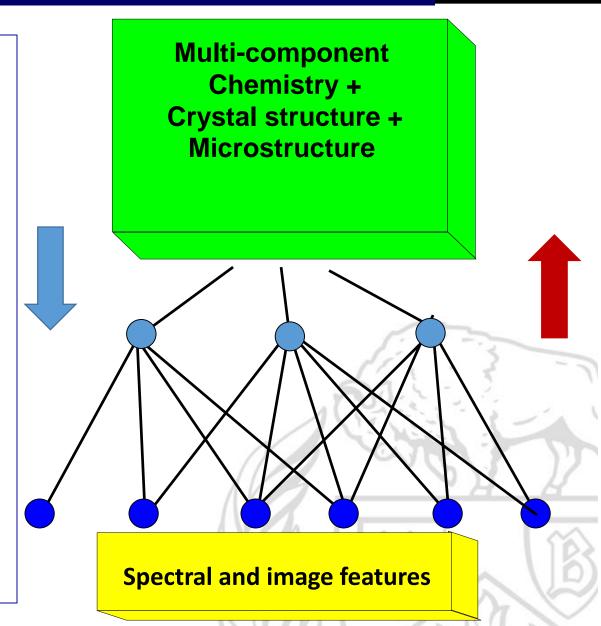
To construct Robust Correlations between chemistry features and image features

Methods:

Data analysis
Statistical learning

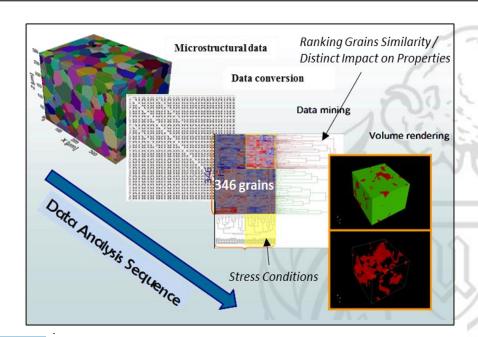
Mechanisms of image /spectral formation

- First principles modeling
- Molecular dynamics



Data Driven Image Based Modeling

<u>Data forms</u>: (i) voxel intensity corresponding to different modalities of imaging (orientation – EBSP, chemical – EDS); (ii) distribution functions of stereological metrics of microstructure (grain size distribution); (iii) discrete data and bounds in discrete data (materials properties); (iv) qualitative data (classes of materials, qualitative processing methods)

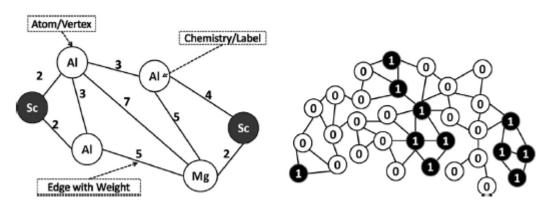


Atom Probe Tomography: the "Hubble" telescope in materials science



A graph-theoretic approach for characterization of precipitates from atom probe tomography data

S. Samudrala ^a, O. Wodo ^a, S.K. Suram ^b, S. Broderick ^b, K. Rajan ^b, B. Ganapathysubramanian ^{a,*}



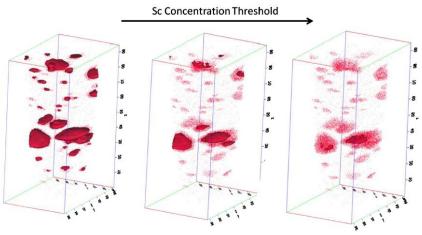


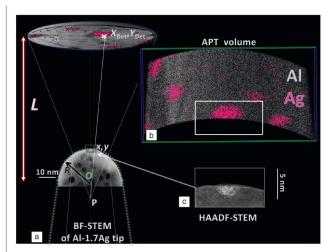
Fig. 13. Concentration isosurfaces of precinitates as a function of Sc concentration threshold value

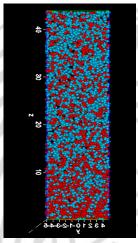
College of Arts and Sciences School of Engineering and Applied Sciences

Advanced volume reconstruction and data mining methods in atom probe tomography

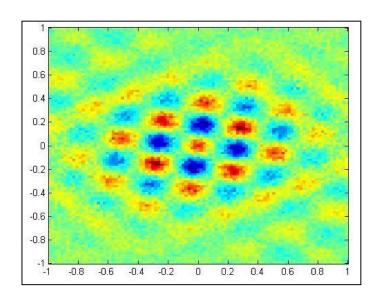
F. Vurpillot, W. Lefebvre, J.M. Cairney, C. Oberdorfer, B.P. Geiser, and K. Rajan

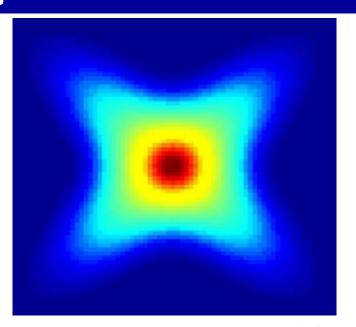
MRS BULLETIN • VOLUME 41 • JANUARY 2016 •





3 D imaging: reaching the limits of imaging





Isolating structural noise via informatics

Microsc, Microanal. 18, 941–952, 2012 doi:10.1017/S1431927612001171 Microscopy Microanalysis

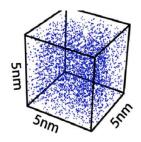
Refining Spatial Distribution Maps for Atom Probe Tomography via Data Dimensionality Reduction Methods

Santosh K. Suram and Krishna Rajan*

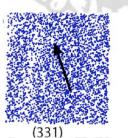


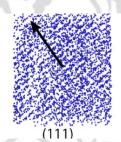
Mining information from atom probe data

Julie M. Cairney ^{ab,e}, Krishna Rajan ^c, Daniel Haley ^{d,e}, Baptiste Gault ^d, Paul A.J. Bagot ^d, Pyuck-Pa Choi ^c, Peter J. Felfer ^{ab}, Simon P. Ringer ^{a,b}, Ross K.W. Marceau ^f, Michael P. Moody ^d



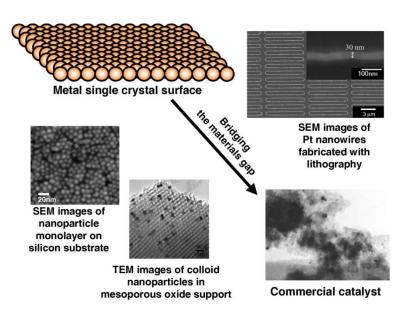


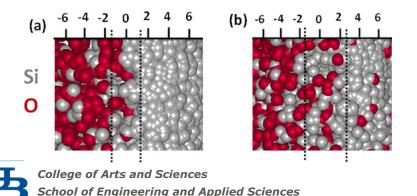


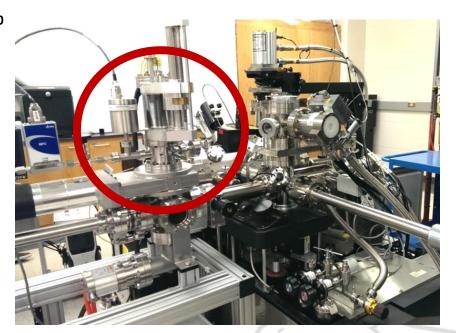


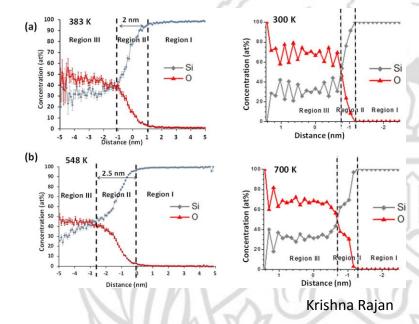
Bridging the Pressure-Materials Gap

G A. Somorjai and J Y. Park Concepts, instruments, and model systems that enabled the rapid evolution of surface science *Surface Science* 603, 1293-1300 (2009)

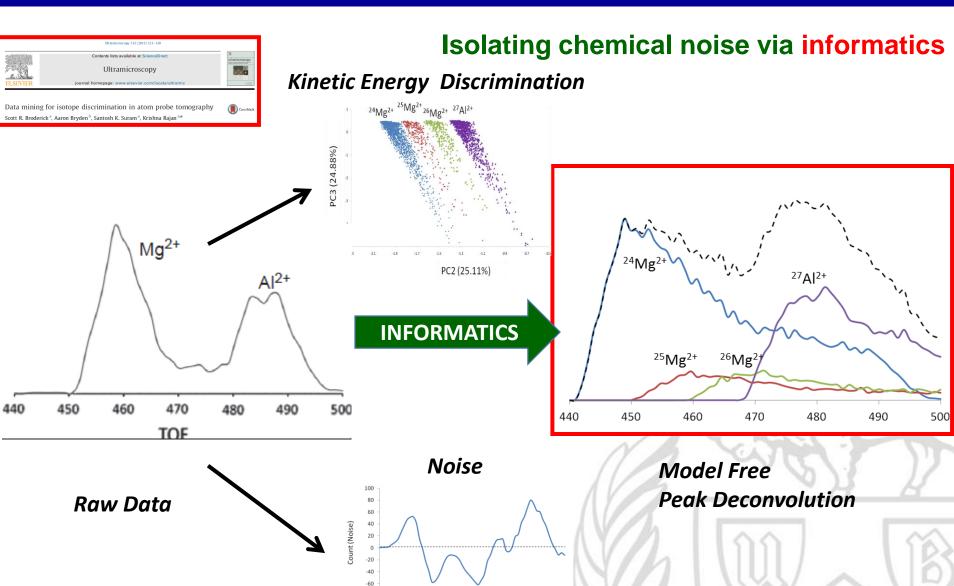








3 D chemical imaging: reaching the limits



TOF

500



Materials Informatics

